

# CS 603: Programming Languages

Lecture 32

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# Overview

- Questions on MP?
- Prolog Semantics continued (starting at 10.2.3 of text)
  - Logical Interpretation
  - Procedural Interpretation

# Logical: How make deterministic?

- *Which* clause  $C \sqsupset D$  do we choose when applying rule **LOGICALQUERY**?
- Given  $g$  and  $G$ , how do we discover a pair of substitutions that cause a match ...?
- Unification

# Logical: Definitions for Unification

- Definition 10.3: A substitution  $\sigma_1$  is *more general* than a substitution  $\sigma_2$  if there exists a  $\sigma_3$  such that  $\sigma_2 = \sigma_3 \circ \sigma_1$ . The more general a substitution is, the fewer things it changes.
- Definition 10.4: *Unification* is the process of finding, for given goals  $g_1$  and  $g_2$ , a substitution  $\sigma$  that unifies  $g_1$  and  $g_2$ . Furthermore,  $\sigma$  must be a *most general* substitution.
- Definition 10.5: A *renaming of variables* is a substitution  $\sigma_\alpha$  in which  $\sigma_\alpha(\text{VAR}(X))$  is always a variable, never an application or an integer.

# Examples of Unification (rule 10.4)

$g_1 = \text{member}(3, [3 | \text{nil}])$

$g_2 = \text{member}(X, [X | L])$

$\square = \{X \mapsto 3, L \mapsto \text{nil}\}$

$g_1 = \text{member}(Y, [3 | \text{nil}])$

$g_2 = \text{member}(X, [X | L])$

$\square = \{X \mapsto 3, Y \mapsto 3, L \mapsto \text{nil}\}$

~~$g_1 = \text{member}(3, [4 | \text{nil}])$~~

~~$g_2 = \text{member}(X, [X | L])$~~

~~$g_1 = \text{length}([3 | \text{nil}], N)$~~

~~$g_2 = \text{member}(X, [X | L])$~~

~~$g_1 = \text{member}(X, [X | L])$~~

~~$g_2 = \text{member}(Y, \text{cons}(\text{mkTree}(1, \text{nil}, \text{nil}), M))$~~

does not unify, as

$\hat{\square}(g_1) = \text{member}(e, [e | L])$

$\hat{\square}(g_2) = \text{member}(e, \text{cons}(\text{mkTree}(e, \text{nil}, \text{nil}), M))$

and  $e$  can never equal  $\text{mkTree}(e, \text{nil}, \text{nil})$

# Motivation for Renaming (rule 10.5)

Given:

```
g = member(M, [1 | nil])
```

```
G = member(X, [X | M])
```

Can these be unified?

What is the problem?

$M$  appears in both  $G$  and  $g$ , but we should be treating these two instances of  $M$  differently. If there were no variables in common, then unification would be easy.

No.

Simple unification doesn't work, as there is no single  $\sigma$  such that  $\hat{\sigma}(G) = \hat{\sigma}(g)$ , since no single substitution can simultaneously satisfy  $M = X$ ,  $X = 1$ , and  $M = \text{nil}$ .

So, rename, then unify.

Accordingly, we change **LOGICALQUERY** to reflect this renaming, then unification

# Procedural Semantics, Version I

We are given database  $D = C_1, \dots, C_n$  and query  $g$ , and wish to know whether  $g$  is satisfied. i.e.  $D \vdash g$ . Search clauses in order; the first time we find a clause with a left hand side matching  $g$ , say  $g :- H_1, \dots, H_m$ , we attempt to satisfy  $H_1, \dots, H_m$ , in that order, following the same procedure for each  $H_j$ .

This only works with *ground* clauses and goals, i.e. those without variables.

# Examples of Procedural Semantics, Version 1

- See 45 I a for examples that work
  - both version 1 and logical
- See 45 I b for examples that don't work
  - under version 1, but do under logical

## What's missing?

Backtracking.

There may be more than one clause that applies to a given goal, and not all applicable clauses lead to a solution.

# Procedural Semantics, Version 2

Search clauses in order; the first time we find a clause  $C_i$  with a left hand side matching  $g$ , say  $g :- H_1, \dots, H_m$ , we attempt to satisfy  $H_1, \dots, H_m$ , in that order, following the same procedure for each  $H_j$ . If all are satisfied,  $g$  has been satisfied. Otherwise, go back to the list of clauses, starting with  $C_{i+1}$ , and look for another clause whose left-hand side equals  $g$ .

This only works with *ground* clauses and goals, i.e. those without variables.

# Examples of Procedural Semantics, Version 1

- See 452a for examples that work
  - both version 2 and logical, but not version 1
- See 452b for examples that don't work
  - under version 1 or 2, but do under logical

## What's the problem?

Infinite loop.

But real Prolog does this too. This is one reason why Logic Programming is not quite Logic.

## What else is missing?

Variables

# Procedural Semantics, Final Version

- See page 453 of textbook