



4. Write a `suffixes` function in ML that works as follows:  
`suffixes [10, 20, 30, 40]` returns `[[10, 20, 30, 40], [20, 30, 40], [30, 40], [40], [ ]]`.
- First write `suffixes` using recursion and pattern matching. Do not use `map`, `foldr`, or `foldl`. **[6 points]**
  - Next write `suffixes` using `map`, `foldr`, and/or `foldl`. Do not use any explicit recursion. **[6 points]**
  - Specify the polymorphic type of the `suffixes` function. **[3 points]**
5. Write a `filter` function in ML that works as follows:  
`filter (fn x => x>0, [3, ~2, 5, 0, 6, ~4, 7])` returns `[3, 5, 6, 7]`.
- First write `filter` using recursion and pattern matching. Do not use `map`, `foldr`, or `foldl`. **[6 points]**
  - Next write `filter` using `map`, `foldr`, and/or `foldl`. Do not use any explicit recursion. **[6 points]**
  - Specify the polymorphic type of the `filter` function. **[3 points]**

6. Write a `superExp` function in ML, such that `superExp(x, k)` computes  $x^{2^k}$ .  
Example: `superExp(3.0, 4)` returns  $3.0^{2^4} = 3.0^{16} = 43046721.0$ . Assume that  $k \geq 0$ . For full credit, make only one recursive call within your function, and do not use any helper functions. Also, your function should be efficient, that is, `superExp(x, k)` should perform a total of only  $k$  multiplication steps. Hints: think of  $x^{2^k}$  as  $(\dots(x^2)^2\dots)^2$ , and use a `let` expression.

a. Write the `superExp` function. **[9 points]**

b. Specify the type of the `superExp` function. **[2 points]**

7. Write a `compare` function in ML that works as follows:  
`compare op<= [1,2,5] [1,3,4]` returns `[Equal, Less, Greater]`.  
`compare (fn ((a,b),(c,d)) => a<=c andalso b<=d)`  
`[(1,2), (3,5), (4,6), (7,8)] [(1,2), (4,6), (3,5), (8,7)]`  
returns `[Equal, Less, Greater, Incompatible]`.

a. First write a datatype that is needed by the `compare` function. **[3 points]**

b. Next write the `compare` function. **[12 points]**

c. Specify the polymorphic type of the `compare` function. **[5 points]**

8. Write a  $\mu$ Smalltalk class called `Interval` such that each instance represents a continuous finite range on the real number line. Here is a client of class `Interval` which illustrates how the class `Interval` should operate. [25 points]

```
(val X (left:right: Interval 0 4)) ; X is the interval 0 ... 4
(val Y (left:right: Interval 2 7)) ; Y is the interval 2 ... 7
(val Z (left:right: Interval 5 11)) ; Z is the interval 5 ... 11
(length X) ; returns 4
(length Y) ; 5
(length Z) ; 6
(disjoint: X Y) ; <False>
(disjoint: X Z) ; <True>
(disjoint: Y X) ; <False>
(disjoint: Y Z) ; <False>
(disjoint: Z X) ; <True>
(disjoint: Z Y) ; <False>
(intersects: X Y) ; <True>
(intersects: X Z) ; <False>
(intersects: Y X) ; <True>
(intersects: Y Z) ; <True>
(intersects: Z X) ; <False>
(intersects: Z Y) ; <True>
```